**Publication Title:** Bi-directional Charging in V2G Systems: An In-Cell Variation Analysis of Vehicle Batteries

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# Bi-directional Charging in V2G Systems: An In-Cell Variation Analysis of Vehicle Batteries

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BMS

DR

EKF

Abstract-Vehicle-to-Grid (V2G) technology enables bi-directional charging of electric vehicle (EV) and facilitates power grid ancillary services. However, battery pack in EV may develop in-cell dynamic variations over time. This is due to the structural complexity and electrochemical operations in the battery pack. These variations may arise in V2G systems due to 1) additional charging and discharging cycles to power grid, 2) external shocks, and 3) long exposures to high temperatures. A particular source of these variations are due to faulty sensors. Therefore, it can be argued that the battery packs in EV are highly reliant on the monitoring of these in-cell variations and their impact of propagation with each involved component. In this paper, a prediction-based scheme to monitor health of variation induced sensors is proposed. Firstly, a propagation model is developed to predict the in-cell variations of a battery pack by calculating the covariance using a median-based expectation. Secondly, a hypothesis model is developed to detect and isolate each variation. This is obtained by deriving a conditional probability-based density function for the measurements. The proposed monitoring framework is evaluated using experimental measurements collected from Li-ion battery pack in electric vehicles. The in-cell variation profiles have been verified using D-SAT Chroma 8000ATS hardware platform. The performance results of the proposed scheme shows accurate analysis of these emerged variations.

*Index Terms*—battery degradation, battery pack voltage, bi-directional charging, cell-to-cell variations, electric vehicles, estimation, expected value, grid-to-vehicle, hypothesis testing, in-cell, Li-ion batteries, median filter, prediction, recursive, smart grid, variation propagation, vehicle-to-grid.

# I. INTRODUCTION

TEHICULAR technologies such as V2G and G2V can smooth the generation ripples of intermittent renewable energy in the electric power grids [1–5]. In particular, the battery packs in electric vehicles (EVs) can be utilized to participate in ancillary services such as demand response (DR) program [6-8]. This owes to the high energy density provided by the mainstream Li-ion batteries, which are facilitated by efficient grid-connected chargers [9, 10]. However, Li-ion battery packs have a complicated structure, and comprises of hundreds of cells. These cells are connected in a circuit combination of series or parallel. The structure becomes more complicated when these arrays of cells-based batteries are equipped with numerous parametric indicators like power capacity, voltage, current, temperature, etc. As a result, the battery pack of an EV is a very sensitive entity as small variations can affect their complicated hierarchy. For instance, the temperature variation serves as an alarming indicator. A rise in temperature due to the frequent charging and discharging may rupture the battery electrolytes, resulting in their decomposition and production of combustible gases. This may also cause fire and thermal runaway [11, 12]. Similarly, a sudden drop in temperature may cause a failure and malfunction of the cathode, leading

EV	Electric Vehicle
KF	Kalman filter
G2V	Grid-to-Vehicle
Li-ion	Lithium ion
MSE	Mean Square Error
PAR	peak-to-average ratio
SoC	State-of-Charge
SoH	State-of-Health
UKF	Unscented Kalman filter
V2G	Vehicle-to-Grid
<b>E</b> <i>u</i>	median expectation operator
$c_{1/2}^{\mu_{1/2}}$	cell 1
c2	cell 2
C	fused form of cells
N	number of in-series connections
Ţ	state of current
F	model metrix
1	transition matrix of temperature
и Г	temperature
1	dynamic variations
B	transition matrices of impedance
ρ ~	impedance
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	standard value of impedence
$C^{z_0}$	transition matrices of poise
G	transition matrices of noise
w +	time instant
l	unic-instant
y	observations output
п	
ν T	observation hoise
1	number of time-instants
p	number of simultaneous observations
$V_1$	input voltage
$V_2$	output voltage
P	covariance matrix
ω	weight
0	difference between individual current estimates
CR	correlated component
UC	uncorrelated component
T	innovation
$\Delta$	perturbation
θ	gradient
$\psi$	data-vector
M	hypothesis model
$S_{\downarrow}$	variance
g(.)	conditional probability density function
j	number of corrupted cells
D	Mahalanobis distance
m	elements in measurement vector

ACRONYMS AND ABBREVIATIONS OF MATHEMATICAL FORMULATIONS

Battery Management System

Demand Response

Extended Kalman filter

to a short-circuit [11, 13, 14]. This may also result in an imprecise calculation of State-of-Charge (SoC), thus amplifying the problems by triggering the overcharge or discharge mechanism [15, 16]. Therefore, an effective Battery Management System (BMS) is required to protect Li-ion battery packs from these issues [17–19]. BMS has also been used to provide diagnostic and prognostic functions at the component-level [18, 19], and at the system-level [20].

Among the published work, data given by sensors to the BMS

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Fig. 1. Proposed in-cell variation and propagation analysis scheme for Li-Ion battery packs

are assumed to be correct. However, this gives rise to the following intriguing questions: 1) Will the installed sensors be able to accurately monitor the incipient in-cell variations happening at pack-level? 2) Do the conventional battery model-based methods [21, 22] take into account the dynamic variations between the composition of two parallel cells, that are connected in a string? Despite of the claimed BMS accuracy in the literature, fewer studies have tested the impact of grid ancillary services on vehicle battery [23, 24]. V2G systems and the ancillary services could introduce performance imperfections in cells, such as: 1) create errors of capacity and power efficiency fade due to cyclic aging, SoC saturation limits, temperature variations, etc. [25], 2) cause random dynamic deviations and offsets of in-cell measurements, and 3) propagation of faults due to these errors and variations. Since each battery pack contains arrays of cells, these deviations will be cultivated and accumulated. This may lead to large differences in the charging capacity of the battery pack, and possibly severe interferences in connections and components of BMS. Reducing these variations is an essential issue for improving the profile and accuracy of BMS, and thus the motivation of this paper. It is beneficial to devise a system-level strategy for variation reduction, which could monitor the consistency of in-cell dynamics and identify the variation sources. This would also promote a data-based solution based on the available online measurements without a conventional battery model. An overlook to incomplete variation analysis can result in oversight of material contamination, voltage leakage and other variations of temperature and conductance.

Therefore, the main contribution is to enhance the observability of the vehicle battery at pack-level in a V2G environment. This is obtained by proposing a prediction-based in-cell variation and propagation analysis. A recursive method is used here to iteratively approximate the distribution of unobserved data. This is achieved by generating recurrence in time series for a more accurate signal analysis. However, unlike the classic recursive filters, which are widely applied for monitoring and estimation applications [20, 26–28], the proposed methodology does not take into account the weighted average between the noisy observations and the prior measurements. Instead, a prediction of cell-dynamics is calculated by re-deriving a medianbased expectation. This is to secure the best possible approximation of the true system, while ensuring a better measure of central tendency in the presence of outliers and small sample size.

To understand the integration of the proposed in-cell variation and propagation analysis into BMS, an overview of the proposed scheme is given in Fig. 1. It shows a V2G system technology setup, where the vehicle battery is utilized for bidirectional charging. In the vehicle battery pack, each set of two parallel cells is called as the floor. The considered scenario assumed that: 1) due to the network of arrays of hundreds of cells, there is no access to the internal states of system, and 2) there is no electromechanical battery model available for the system. The proposed scheme is able to provide the dynamic aspects of component interactions. Note the main focus of this paper is to propose an in-cell variation and propagation analysis for a vehicle battery pack. This has been achieved by demonstrating the proposed scheme at a constant operating environment temperature of  $20^{\circ}C$  with a single frequency. Moreover, only two parallel cells connected in a thread of series are considered here, which is the standard structure used in Li-ion battery packs [29].

The formation of paper is as follows: The proposed scheme is discussed in Section II. The implementation and evaluation of the scheme is made in Section III. Finally, conclusions are drawn in Section IV.

**Notations:** In this paper, a structured notation scheme is defined.  $\mathbf{E}_{\mu_{1/2}}$  is the median expectation operator. A symbol ~ over a variable denotes the sample median of the variable, e.g.  $\tilde{I}$  is the median of I. A hat over a variable represents an estimate of the variable, e.g.  $\hat{I}$  is an estimate of I.  $\mu_{1/2}$  is denoted as the sample size median. The individual entries of a variable like I are denoted by I(l). When any of these variables becomes a function of time, the time index t appears as a subscript (e.g.  $I_t$ ,  $H_t, y_t$ ). The notation  $I_0^T$  is used to represent the sequence (e.g.



Fig. 2. Seven step-based formulation framework of the proposed scheme



Fig. 3. Variation and propagation in a time-variant process

 $I_0, I_1, ..., I_T$ ).

# **II. PROPOSED SCHEME**

The proposed scheme comprises of a formulation framework which involves seven steps.

# A. Seven-Step Based Formulation Framework

The seven-step based formulation framework is illustrated in Fig. 2. It summarizes the formulation and equations involved at each step as follows: 1) The proposed methodology begins with developing an in-cell variation propagation model. The assumed system model considered an array of parallel cells connected in a string of series. 2) A relationship between battery parameters in a battery pack is developed. The prediction-based estimation methodology is then built on it for calculating both the 3) fused, and the 4) in-cell current variations respectively. The diagnosis of vehicle battery pack is made by 5) extracting the residual vector, 6) conditional probability-based hypothesis testing, and 7) validation gate.

Note that a standard Li-ion vehicle battery-pack structure of

two parallel cells connected in a thread of N number of series is considered [29]. In this structure, the in-cell variations are dependent on the split of current between two parallel cells. Thus, the variation model is built on the state current  $I_t$ .

1) Step 1 - Variation and Propagation Model: Consider a discrete-time dynamical model of a vehicle battery-pack involving cells c1 and c2. These cells are connected in parallel with a voltage supply to N number of in-series connections at time-instant t. The cell dynamics always have variations in a time-variant process. This can be further expressed in Fig. 3. At time-instant t, the cell dynamics are represented by state of current  $I_t$ , and the observations output  $y_t$ . As it is a timevariant process, the cell-dynamics will show variations at each instant. The main variation inputs consist of  $\alpha_t$ ,  $\beta_t$  and  $G_t$ , which present the transition matrices of temperature, impedance and noise respectively.  $I_t$  is related to the deviation of measurements in  $y_t$  with  $F_t$  and  $H_t$ , which represents the modal matrix and mapping observation matrix respectively. T refers to the number of time-instants. A state difference equation can be further described in the deviation propagation as:

$$I_{t+1}^{\mathcal{C}} = F_t^{\mathcal{C}} I_t^{\mathcal{C}} + \frac{\alpha_t^{\mathcal{C}}}{2} (\Gamma_t^{c1} + \Gamma_t^{c2}) I_t^{var} + \beta_t^{\mathcal{C}} (z_t^{c1} + z_t^{c2}) I_t^{var} + G_t^{\mathcal{C}} w_t^{\mathcal{C}} (1)$$

$$y_t^{\mathcal{C}} = H_t^{\mathcal{C}} F_t^{\mathcal{C}} I_t^{\mathcal{C}} + \nu_t^{\mathcal{C}}$$
(2)

where the superscript c1 represents cell 1, and superscript c2denotes cell 2. The symbol C is used to present the fused form of cells c1 and c2, i.e. C = c1 + c2, whereas C' presents the transpose of this fused form. The symbol var presents the dynamic variations in cells. The  $I_0^{\mathcal{C}} \in \mathbf{R}^r$  represents an initial condition of the current state,  $F_t^{\mathcal{C}} \in \mathbf{R}^{r \times r}$  is a modal matrix of the state response of current, such that it depends on covariates,  $\alpha_t^{\mathcal{C}} \in \mathbf{R}^{r \times r}$  is the transition matrix of temperatures  $\Gamma_t^{c1} \in \mathbf{R}^r$ and  $\Gamma_t^{c2} \in \mathbf{R}^r$  of cells c1 and c2 respectively. Also,  $\beta_t^{\mathcal{C}} \in \mathbf{R}^{r \times r}$  is the impedance transition matrix of impedances  $z_t^{c1} \in \mathbf{R}^r$  and  $z_t^{c2} \in \mathbf{R}^r$  respectively.  $G_t^{\mathcal{C}} \in \mathbf{R}^{r \times r}$  is the noise transition matrix, which can be defined as a probability vector, whose elements are non-negative real numbers and sum to 1.  $w_t^{\mathcal{C}} \in \mathbf{R}^r$  is the random process noise. In the observation model (2),  $y_t^{\mathcal{C}} \in \mathbf{R}^p$  is the observation output of state of current, p is the number of simultaneous observations for estimation made at time-instant t,  $H_t^{\mathcal{C}} \in \mathbf{R}^{p \times r}$  is the observation matrix of current state,  $I_t^{\mathcal{C}}$  is the current state matrix, and  $\nu_t^{\mathcal{C}} \in \mathbf{R}^p$  is the observation noise. Note the noises  $w_t$  and  $\nu_t$  have been assumed initially uncorrelated zero-median white Gaussian<sup>1</sup>.

2) Step 2 - Relationship between Battery Parameters: Once the observation model is extracted, the battery parameters and their interrelations collected from sensors are formulated. Note the battery cells are considered here as conducting bodies only. The known parameters of floor of parallel cells connected in a series string are: 1) string voltages, 2) string temperature, and 3) string current.

At time-instant t, current of individual cells c1 and c2 can be represented as the difference between input voltage  $V_{1,t}^{\mathcal{C}}$ and output voltage  $V_{2,t}^{\mathcal{C}}$ , with respect to the individual cell

<sup>&</sup>lt;sup>1</sup> White Gaussian is used as an additive to represent a basic noise model. It is represented as Gaussian to portray the effect of random processes. To cover the domain of all possible random processes, it has a normal distribution and uniform power frequency (white) [30]. The median time-domain value for such a distribution is considered here to be zero.

$$I_t^{c1} = \frac{V_{1,t}^{\mathcal{C}} - V_{2,t}^{\mathcal{C}}}{z_t^{c1}}, I_t^{c2} = \frac{V_{1,t}^{\mathcal{C}} - V_{2,t}^{\mathcal{C}}}{z_t^{c2}}$$
(3)

where  $I_t^{c1}$  and  $I_t^{c2}$  are the individual readings from the current sensor at cells c1 and c2 respectively. Also, impedances  $z_t^{c1}$  and  $z_t^{c2}$  for cells c1 and c2 are:

$$z_t^{c1} = z_t^{c1^0} + \left[1 + \alpha_t^{\mathcal{C}} (\Gamma_t^{c1} - \Gamma_t^{c1^0})\right], \tag{4}$$

$$z_t^{c2} = z_t^{c2^0} + \left[ 1 + \alpha_t^{\mathcal{C}} (\Gamma_t^{c2} - \Gamma_t^{c2^0}) \right]$$
(5)

where  $z_t^{c10}$  and  $z_t^{c20}$  are the standard values of impedance at room temperature  $\Gamma_t^{c10}$  and  $\Gamma_t^{c20}$  respectively.  $\alpha_t^{\mathcal{C}}$  is the transition matrix of temperature at cells c1 and c2.

Note  $\Gamma_t^{\mathcal{C}}$  is assumed here as an average value of temperature for cells c1 and c2. Thus, the general relation between battery parameters can be expressed as:

$$\Gamma_t^{\mathcal{C}} = \frac{z_t^{c1}}{2\alpha_t^{\mathcal{C}} z_t^{c1^0}} + \frac{z_t^{c2}}{2\alpha_t^{\mathcal{C}} z_t^{c2^0}} + \frac{\Gamma_t^{c1^0}}{2} + \frac{\Gamma_t^{c2^0}}{2} - \frac{1}{\alpha_t^{\mathcal{C}}} \tag{6}$$

Once the dynamic relationships between the parameters of the vehicle battery are determined, variation and propagation model is further derived to calculate the covariance matrix. This is a challenging task due to 1) the absence of a battery model, where accuracy of the variation estimation is dependent on the parameters of interaction between cells, and 2) considering the median-based expectation over the classic weighted average to calculate the noisy observations and prior measurements.

3) Step 3 - Prediction of Fused Current Variations: Based on the formulated propagation and observation models, the fused current prediction can be derived by the covariance between the cells c1 and c2. This required some additional properties of median expectation from [20].

Assume  $\hat{I}_{t|t}^{\mathcal{C}}$  as the estimated state at time-instant t for the time-sequence T. Given the observation model of (2) and timesequence T-1, the state prediction of current can be defined. This definition is linearly expressed with a conditional probability as:

$$\hat{I}_{t|t-1}^{\mathcal{C}} = \mathbf{E}_{\mu_{1/2}} [I_t^{\mathcal{C}} | y_{T-1}^{\mathcal{C}}] + \mathbf{E}_{\mu_{1/2}} [I_t^{var} | I_t^{\mathcal{C}}] 
= F_t^{\mathcal{C}} \arg\min_{I^{\mathcal{C}}} [I_{t-1}^{\mathcal{C}} - \mu_{1/2,t-1}] + \left(\frac{\alpha_t^{\mathcal{C}}}{2} (\Gamma_t^{c1} + \Gamma_t^{c2}) + \beta_t^{\mathcal{C}} (z_t^{c1} + z_t^{c2})\right) \arg\min_{I^{var}} [I_{t-1}^{var} - \mu_{1/2,t-1}]$$
(7)

Taking the difference between (1) and (7) gives:

 $\tau C \hat{\tau} C$ 

$$\begin{split} & I_t^- - I_{t|t-1} \\ &= F_t^{\mathcal{C}} I_t^{\mathcal{C}} + \frac{\alpha_t^{\mathcal{C}}}{2} \left( \Gamma_t^{c1} + \Gamma_t^{c2} \right) I_t^{var} + \beta_t^{\mathcal{C}} (z_t^{c1} + z_t^{c2}) I_t^{var} + G_t^{\mathcal{C}} w_t^{\mathcal{C}} \\ &- F_t^{\mathcal{C}} \arg\min_{I^{\mathcal{C}}} [I_{t-1}^{\mathcal{C}} - \mu_{1/2,t-1}] \\ &- \frac{\alpha_t^{\mathcal{C}}}{2} \left( \Gamma_t^{c1} + \Gamma_t^{c2} \right) \arg\min_{I^{var}} [I_{t-1}^{var} - \mu_{1/2,t-1}] \\ &- \beta_t^{\mathcal{C}} (z_t^{c1} + z_t^{c2}) \arg\min_{I^{var}} [I_{t-1}^{var} - \mu_{1/2,t-1}] \\ &= F_t^{\mathcal{C}} (I_{t-1}^{\mathcal{C}} - \arg\min_{I^{\mathcal{C}}} [I_{t-1}^{\mathcal{C}} - \mu_{\frac{1}{2},t-1}]) + G_t^{\mathcal{C}} w_t^{\mathcal{C}} \\ &+ \frac{\alpha_t^{\mathcal{C}}}{2} (\Gamma_t^{c1} + \Gamma_t^{c2}) (I_t^{var} - \arg\min_{I^{var}} [I_{t-1}^{var} - \mu_{1/2,t-1}]) \\ &+ \beta_t^{\mathcal{C}} (z_t^{c1} + z_t^{c2}) (I_t^{var} - \arg\min_{I^{var}} [I_{t-1}^{var} - \mu_{1/2,t-1}]) \end{split}$$

Here  $I_t^{\mathcal{C}} - \hat{I}_{t|t-1}^{\mathcal{C}} = P_{I,t|t-1}^{\mathcal{C}}$ , where  $P_{I,t|t-1}^{\mathcal{C}}$  represents the covariance matrix. Taking the median-based expected value for (8) gives:

$$P_{I,t|t-1}^{\mathcal{C}} = F_t^{\mathcal{C}} P_{\mu_{1/2,t-1|t-1}}^{\mathcal{C}} F_t^{\mathcal{C}'} + \frac{\alpha_t^{\mathcal{C}}}{2} P_{\mu_{1/2,t-1|t-1}}^{var,\Gamma} \frac{\alpha_t^{\mathcal{C}}}{2} + \beta_t^{\mathcal{C}} P_{\mu_{1/2,t-1|t-1}}^{var,z} \beta_t^{\mathcal{C}'} + G_t^{\mathcal{C}} Q_t^{\mathcal{C}} G_t^{\mathcal{C}'}$$
(9)

The estimated state  $\hat{I}_t^{\mathcal{C}}$  and the covariance matrix  $P_{I,t}^{\mathcal{C}}$  represent the measurement updated equations, which were derived from the first principles based on (7) to (9). However,  $P_{I,t}^{\mathcal{C}}$  assumes that both cells have the same dynamics, i.e. the same 1) impedance, 2) operating temperature, and 3) other cell dynamics. This motivates to consider the problem for vehicle battery pack with dynamic in-cell variations.

4) Step 4 - Prediction of in-Cell Current Variations: The in-cell variations narrate the dynamics of the individual cells. These are primarily due to the factors, such as: 1) total capacity of cell, 2) internal resistance of cell, and 3) the initial value of SoC, which gives an adequate reason to derive a covariance matrix. This covariance matrix can further represent the dynamical situation of in-cell current estimation. Let  $P_{I,t|t}^{c1}$  be the conservative covariance estimate of cell c1, such that  $P_{I,t|t}^{c1} \ge \mathbf{E}_{\mu_{1/2}} \Big[ \Big( \mu_{1/2,t|t}^{c1} - \mathbf{E}_{\mu_{1/2,t|t}} (I_{t|t}^{\mathcal{C}}) \Big) \Big( \mu_{1/2,t|t}^{c1} - \mathbf{E}_{\mu_{1/2,t|t}} (I_{t|t}^{\mathcal{C}}) \Big) \Big]$  $\mathbf{E}_{\mu_{1/2,t|t}}(I_{t|t}^{\mathcal{C}}))$ , where  $\mu_{1/2,t|t}^{c1}$  is the median vector for current at cell c1. Note to achieve convergence, the estimated covariance of cell c1,  $P_{I,t|t}^{c1}$  follows a behavior as: 1) to always calculate an over-estimate of the median-based expected squared difference between the true median of the unknown distribution function of cell c1,  $\mu_{1/2}^{c1}$ , and its estimate  $\arg \min[I_{t-1}^{c1} \mu_{1/2,t-1}^{c1}$ ], 2) to assign a weight  $\omega$  to calculate the split of in-cell current variations among the parallel connection, 3) this weight is then computed in order to determine the trace of split of current, thereby assigning an estimate value to the individual current estimates  $\hat{I}_{t|t}^{c1}$  and  $\hat{I}_{t|t}^{c2}$  respectively.

$$\hat{I}_{t|t}^{\mathcal{C}} = P_{I,t|t}^{\mathcal{C}} \left( \omega P_{I,t|t}^{c1^{-1}} (F_{t}^{\mathcal{C}} \hat{I}_{t|t}^{c1} \frac{\alpha_{t}^{\mathcal{C}}}{2} \Gamma_{t}^{c1} \beta_{t}^{\mathcal{C}} z_{t}^{c1}) + (1-\omega) P_{I,t|t}^{c2^{-1}} (F_{t}^{\mathcal{C}} \hat{I}_{t|t}^{c2} \frac{\alpha_{t}^{\mathcal{C}}}{2} \Gamma_{t}^{c2} \beta_{t}^{\mathcal{C}} z_{t}^{c2}) \right)$$
(10)

where the difference between  $\hat{I}_{t}^{c1}$  and  $\hat{I}_{t}^{c2}$  can be expressed by  $\delta_t^{\mathcal{C}}$  as follows:

$$\hat{I}_{t|t}^{c1} - \hat{I}_{t|t}^{c2} \tag{11}$$

 $\delta^{\mathcal{C}}_t = \hat{I}^{c1}_{t|t} - \hat{I}^{c2}_{t|t} \tag{11}$  The expression (11) can be normalized further. This is done by using median-based expectation operator as:

$$\mathbf{E}_{\mu_{1/2}}[\delta_t^{\mathcal{C}} \delta_t^{\mathcal{C}'}] = \mathbf{E}_{\mu_{1/2}}[\hat{I}_{t|t}^{c1} - I_{t|t}^{\mathcal{C}} - (\hat{I}_{t|t}^{c2} - I_{t|t}^{\mathcal{C}})][\hat{I}_{t|t}^{c1} - I_{t|t}^{\mathcal{C}} - I_{t|t}^{\mathcal{C}})]$$
(12)

and is equivalent to:

$$\mathbf{E}_{\mu_{1/2}}[\delta_t^{\mathcal{C}} \delta_t^{\mathcal{C}'}] = P_{I,t|t}^{c1} + P_{I,t|t}^{c2} - P_{I,t|t}^{\mathcal{C}} - P_{I,t|t}^{\mathcal{C}}$$
(13)

The term  $P_{I,t|t}^{\mathcal{C}}$  denotes the associated covariance of fused current with its estimate  $\hat{I}_{t|t}^{\mathcal{C}}$ . Also,

 $P_{I,t|t}^{\mathcal{C}} = \mathbf{E}_{\mu_{1/2}}[(\hat{I}_{t|t}^{c1} - I_t^{\mathcal{C}})(\hat{I}_{t|t}^{c2} - I_t^{\mathcal{C}})'] = \mathbf{E}_{\mu_{1/2}}[\tilde{I}_{t|t}^{c1}\tilde{I}_{t|t}^{c2}] = P_{I,t|t}^{\mathcal{C}'}(14)$ where  $P_{I,t|t}^{\mathcal{C}}$  is the correlation between the two current estimates  $\hat{I}_t^{c1}$  and  $\hat{I}_t^{c2}$ , respectively. Similarly, according to (10),  $P_{I,t|t}^{\mathcal{C}}$  can



Fig. 4. Setup for V2G bi-directional charging system

be represented in the form of  $P_{I,t|t}^{c1}$  and  $P_{I,t|t}^{c2}$  as:

$$P_{I,t|t}^{\mathcal{C}} = \frac{2P_{I,t|t}^{c1}P_{I,t|t}^{c2}}{F_t^{\mathcal{C}}\alpha_t^{\mathcal{C}}\beta_t^{\mathcal{C}}\left(\omega\Xi_t^{c1} + (1-\omega)\Xi_t^{c2}\right)}$$
(15)

where  $\Xi_t^{c1} = P_{I,t|t}^{c1} I_{t|t}^{c1} \Gamma_t^{c1} z_t^{c1}$  and  $\Xi_t^{c2} = P_{I,t|t}^{c2} I_{t|t}^{c2} \Gamma_t^{c2} z_t^{c2}$ . However, there is a value for trace of split of current, which is dependent on variants of 1) change in temperature, 2) voltage fluctuation, and 3) external disturbances. Let the current at cell c1,  $I^{c1}$  consists of a correlated component  $I_{C\mathcal{R}}^{c1}$  and an uncorrelated component  $I_{\mathcal{UC}}^{c1}$  with respect to cell c2, such that  $I^{c1} = I_{C\mathcal{R}}^{c1} + I_{\mathcal{UC}}^{c1}$ , then the estimated covariance matrices for  $I_{C\mathcal{R}}^{c1}$  and  $I_{\mathcal{UC}}^{c1}$  will be  $P_{I,C\mathcal{R}}^{c1}$  and  $P_{I,\mathcal{UC}}^{c1}$  respectively. This gives a new definition of covariance matrices for cells c1 and c2 as:

$$P_{I,t|t}^{c1} = \frac{P_{I,C\mathcal{R},t|t}^{c1}}{\omega} + P_{I,\mathcal{UC},t}^{c1}, P_{I,t|t}^{c2} = \frac{P_{I,C\mathcal{R},t|t}^{c2}}{1-\omega} + P_{I,\mathcal{UC},t}^{c2}$$
(16)

Here  $\omega$  can also be determined by optimizing an objective function in terms of  $\omega$ , such that  $\omega \in [0, 1]$ . One of the possibilities of such an occurrence could be as the determinant of new covariance [31]. This gives the fused form of covariance matrices for cells c1 and c2. Representing in the form of correlated and uncorrelated current estimate measurements, it can be written as:

$$P_{I,C\mathcal{R},t|t}^{\mathcal{C}} = P_{I,t|t}^{\mathcal{C}} - P_{I,C\mathcal{R},t|t}^{\mathcal{C}}$$
(17)  
$$P_{I,\mathcal{UC},t|t}^{\mathcal{C}} = P_{I,t|t}^{\mathcal{C}} \left( P_{I,t|t}^{c1^{-1}} P_{I,\mathcal{UC},t|t}^{c1} P_{I,t|t}^{c1^{-1}} + P_{I,t|t}^{c2^{-1}} P_{I,\mathcal{UC},t|t}^{c2^{-1}} \right) P_{I,t|t}^{\mathcal{C}}$$
(18)

Considering the correlated and uncorrelated measurements from cells c1 and c2 in (16), (10) becomes:

$$\hat{I}_{t|t}^{\mathcal{C}} = P_{I,t|t}^{\mathcal{C}} \left[ \omega(\frac{\omega}{P_{I,\mathcal{CR},t|t}^{c1} + P_{I,\mathcal{UC},t|t}^{c1}}) \hat{I}_{t|t}^{c1} + (1-\omega)(\frac{1-\omega}{P_{I,\mathcal{CR},t|t}^{c2} + P_{I,\mathcal{UC},t|t}^{c2}}) \hat{I}_{t|t}^{c2} \right]$$
(19)

(19) can be further developed as:

$$\hat{I}_{t|t}^{\mathcal{C}} = \left(\frac{\omega^2 F_{t|t}^{\mathcal{C}} \hat{I}_{t|t}^{c1} P_{I,t|t}^{\mathcal{C}}}{P_{I,\mathcal{C}\mathcal{R},t|t}^{c1} + P_{I,\mathcal{U}\mathcal{C},t|t}^{c1}}\right) + \left(\frac{(1-\omega)^2 F_{t|t}^{\mathcal{C}} \hat{I}_{t|t}^{c2} P_{I,t|t}^{\mathcal{C}\mathcal{R}}}{P_{I,\mathcal{C},t|t}^{c2} + P_{I,\mathcal{U}\mathcal{C},t|t}^{c2}}\right) (20)$$

Taking the feedback for the update of current-split estimate gives,

$$P_{I,t|t}^{\mathcal{C}^{-1}} \hat{I}_{t|t}^{\mathcal{C}} = -(N-1) P_{I,t|t}^{\mathcal{C}^{-1}} \hat{I}_{t|t}^{\mathcal{C}} + \left( \frac{\omega^2 F_{t|t}^{\mathcal{C}} I_{t|t}^{c1} P_{t|t}^{\mathcal{C}}}{P_{I,\mathcal{C}\mathcal{R},t|t}^{c1} + P_{I,\mathcal{U}\mathcal{C},t|t}^{c1}} \right) \\ + \left( \frac{(1-\omega)^2 F_{t|t}^{\mathcal{C}} \hat{I}_{t|t}^{c2} P_{I,t|t}^{\mathcal{C}}}{P_{I,\mathcal{C}\mathcal{R},t|t}^{c2} + P_{I,\mathcal{U}\mathcal{C},t|t}^{c2}} \right)$$
(21)

where in-cell current variations can be iteratively updated at each time-instant t. N = 2 denotes the number of cells. The proof of convergence for covariance of in-cell current variations (20)-(21) are as follows.

**Proof:** This is proved in the Appendix.

Once the prediction of fused and in-cell variations have been calculated for estimation, a residual vector is generated to detect the variations.

5) Step 5 - Determination of Residual Vector: The residual of the estimated parameters is usually calculated to detect any 1) system-bias variation, and 2) sensor faults. These deviants could be detected for each measurement by (2). The representation for cells c1 and c2 can be made as:

$$y_t^{c1} = H_t^{c1} F_t^{c1} I_t^{c1} + \nu_t^{c1}$$
(22)

$$y_t^{c2} = H_t^{c2} F_t^{c2} I_t^{c2} + \nu_t^{c2}$$
(23)

Based on (22)-(23), a number of observations for N number of cells can be taken. Considering cell c1, the difference between the predicted output and the observations is calculated as:

$$\begin{split} & \boldsymbol{\Upsilon}_{t+1}^{c1} = [y_{t+1}^{c1} - \hat{y}_{t+1}^{c1}] = \boldsymbol{\Sigma}_{t=1}^{T} \boldsymbol{\psi}_{t-1}^{'} \boldsymbol{\theta}_{t}^{c1^{(1)}} \boldsymbol{\Delta} I_{t}^{c1} + \boldsymbol{\nu}_{t}^{c1} ~~(24) \\ & \text{where, the vector}~ \boldsymbol{\Upsilon}_{t+1}^{c1} ~~\text{is the innovation calculated for cell $c1$.} \\ & \boldsymbol{\Delta} I_{t} = I_{t}^{f} - I_{t} ~~\text{is the perturbation in}~ I^{c1}. ~~y_{t}^{c1} ~~\text{is the fault-free} \\ & (\text{nominal) output.}~ y_{t}^{c1^{f}} ~~\text{is the faulty output.}~ \boldsymbol{\theta}_{t}^{c1^{(1)}} = \frac{\delta \boldsymbol{\theta}_{t}}{\delta I_{t}^{c1}}, ~~\text{and}~ \boldsymbol{\psi} \end{split}$$



Fig. 5. Measurements of total a) voltage, b) temperature, and c) current. Measurements of current profile for cells d) c1, c2, e) c3, c4, f) c5, c6, g) c7 and c8 of Li-ion battery pack. MSE performance of current estimate in cells h) c1 and i) c2. Comparison of j) current profile in faulty cell c2, k) its estimate, and l) evaluation of residual signal

is the data vector formed of the past outputs and past reference inputs of cell c1. The gradient  $\theta_t$  was estimated by performing a number of offline experiments for the cell c1. The input-output data from all the perturbed parameter experiments were then used to identify the gradients of cell c1,  $\theta_t^{c1^{(1)}}$ . The outcome could be represented in the form of a density function between the faulty data and fault-free data. The variance  $S_{t+1}$  of this innovation can be found from (22) for cell c1 as:

$$S_{t+1}^{c1} = \mathbf{E}_{\mu_{1/2}}(y_{t+1}^{c1}y_{t+1}^{c1})$$
  
=  $F_t^{c1}P_{\mu_{1/2,t-1|t-1}}^{c1}F_t^{c1'} + \frac{\alpha_t^{c1}}{2}P_{\mu_{1/2,t-1|t-1}}^{var,\Gamma}\frac{\alpha_t^{c1'}}{2}$   
+  $\beta_t^{c1}P_{\mu_{1/2,t-1|t-1}}^{var,z}\beta_t^{c1'} + G_t^{c1}Q_t^{c1}G_t^{c1'}$  (25)  
which shows the innovation covariance for cell  $c1$ .

Once the residuals vector  $\Upsilon_{t+1}^{c1} = y_{t+1}^{c1} - \hat{y}_{t+1}^{c1}$  is yielded by comparing the estimation vector  $\hat{y}_t^{c1}$  with the measurements vector  $y_t$ , the fault isolation module is processed using the hypothesis model.

6) Step 6 - Conditional Probability-based Hypothesis Model: The conditional probability is developed using the hypothesis model  $M_t$ . The model represents the nominal (fault-free) operating mode of the cells at time t + 1 given the expression for cell c1 as:

$$p_{I,t}(y_t^{\mathcal{C}}) = \frac{g(y_{t+1}^{\mathcal{C}}|M_t^{c1}, [y_t...y_T])p_{I_t}(y_t^{c1})}{\sum_{j=0}^n (g(y_{t+1}^{\mathcal{C}}|M_t^{c_j}, [y_t...y_T])p_{I_t}(y_t^{c_j})}$$
(26)

In (26), g(.) is the conditional probability density function of the measurement  $y_{t+1}$ , which is conditioned on the model  $M_t$ and the previous measurements. j is the number of corrupted cells from 0 to n. This function is determined by the expression for cell c1 as:

$$g(y_{t+1}^{\mathcal{C}}|M_t^{c1}, [y_t, ..., y_T]) = \frac{e^{-\frac{1}{2}D_{t+1}^{c1}}}{(2\pi)^{\frac{m}{2}}|S_{t+1}^{c1}|^{\frac{1}{2}}}$$
(27)

 $D_{t+1}$  is the Mahalanobis distance at time t+1, which can be defined as the dissimilarity measure between the nominal (fault-free) and the faulty operating mode. m is the number of elements in the measurement vector.

The hypothesis model helps to process a validation gate for fault location.

7) Step 7 - Validation Gate: At each measurement collected from cells c1 and c2, a validation gate can be generated. It can be expressed for cell c1 as:

$$\Upsilon_{t+1}^{c1} S_{t+1}^{c1^{-1}} \Upsilon_{t+1}^{c1^{-1}} = Q_t^{c1}$$
(28)

where (28) can be used to test observations for each cell in the circuit in order to determine the fault location.

### **III. IMPLEMENTATION AND EVALUATION**

The proposed scheme was evaluated on a vehicle Li-ion battery-pack. The scheme was operated under different operating conditions. The experiments were conducted based on the guidelines issued by United States Department of Energy battery test manual [32, 33]. The profiles of fault propagation were verified using D-SAT Chroma 8000ATS hardware platform. In order to evaluate the proposed methodology, a test case has been designed as shown in Fig. 4. The test case represents V2G bidirectional charging environment. The test case is dependent on the setup of floor combination of parallel cells, which are connected in a string of series. The online values of all the cells connected in this structure are plotted in Fig. 5, where Fig. 5 (a-



Fig. 6. Evaluation of fault a) isolation, and b-i) localization for injected reverse polarity fault in cell c2

c) shows the profiles of total voltage, total temperature and total current respectively. Fig. 5 (d-g) represents the current values of each cell in the floor. The test case considered a propagated reverse polarity fault in Fig. 1 with effect on cell c2. The proposed method is referenced with two mainstream techniques: 1) Extended Kalman filter (EKF) [34, 35], and 2) Particle filter (PF) [36]. The characterized battery cell considered has a nominal capacity of 2.3 Ah and a nominal voltage of 3.2 V. The experimental setup for verifying the fault propagation during bidirectional charging is composed of: 1) a D-SAT Chroma battery cell simulator with charging capacity of 2160 KWh, 2) an NXP BMS controller, 3) a DC motor, 4) a labVIEW-based compaqRIO controller for the motor, 5) a DC generator, 6) a boost DC-DC converter with a resonant circuit for a soft-switching and operation, 7) a programmable electronic load, 8) a data acquisition unit for collecting measurement signals, 9) data storage, and 10) a computer for controlling the current load and supply. The following tests were conducted with a frequency of 10 Hz at 20  ${}^{0}C$ : 1) characterization test, and 2) driving cycle test. The current is considered to be positive at discharge and negative at charge. Note the implementation was tested offline. This is because of two main reasons: 1) An injected fault can be detected by a BMS, which may result in compensation of the fault or system shutdown. 2) If the BMS is unable to detect the fault, the injected fault may result in potential damage to vehicle battery. These reasons may provide hinderance to the proposed scheme while testing the whole set of considered fault situations. Therefore, the off-line approach has been chosen. Note the focus of this paper is to make an in-cell variation propagation analysis.

The purpose of this study is to examine the estimation and propagation analysis capability of the proposed scheme. A standard estimation analysis with no faults was made on the floor of cells c1 and c2. This was an initial analysis made to evaluate the performance of the proposed scheme towards estimating the regular cell dynamics without any injection. The current profiles of cells c1 and c2 were estimated. A comparison of mean square error (MSE) between the main stream EKF [34, 35], PF [36], and the proposed filter is shown in Fig. 5 (h)-(i). All the techniques performed reasonably well. However, the EKF started with a slow time tracking response, causing it to have a higher MSE value in the initial time windows. This is due to the lack of abrupt response in updating the covariance matrix at every iteration. This was due to the initialization procedure of EKF. This is not the case for PF. It performed better than EKF. However, the initial overshoot was not well-captured by the PF. This is due to its non-deterministic nature towards abrupt variations. In contrast, the proposed filter was fast enough to capture the dynamics well from the start.

Once a standard estimation analysis has been made, a test case was generated to evaluate the performance of the proposed filter in the presence of an injected fault. Cell c2 suffered from a reverse polarity fault in the middle of the charging cycle from 6.0-9.0 h as shown in Fig. 5 (j). This could be possibly due to an operational fault in BMS caused by a shorted diode inside the cell. This may also reverse the electro-mechanical process and an acceleration in current flow, resulting in high electrical leakage among the cells and the circuit. This could possibly lead to burnout due to a thermal run-away chain reaction and a shorted capacitor [37]. A comparison of estimates between the main stream PF [36] and the proposed scheme can be seen in Fig. 5 (k). The proposed method gives more accurate results than PF. It also managed to estimate the deviations of the profile with precision. This is due to its predictive nature using the innovation process used for the initialization. Furthermore, fault detection has been made by generating a residual vector to calculate variations between the fault-free and faulty profile of the cell c2. The threshold selected for current was  $\pm 1$ . Referring to Fig.5 (l), the fault was detected using the threshold selection. Fault isolation and localization can be observed in Fig. 6 (a) and Fig. 6 (g-i) respectively. By applying conditional probabilitybased hypothesis model and validation gate, the operator can clearly analyze the fault occurrence in cell c2.

The faulty cell c2 also made a propagation impact on other parameters of the circuit as follows:

- First Propagation: A step-like rise in voltage  $V_{2,t}$  is noticed from 6.0 to 9.1 h.
- Second Propagation: A spike variation in temperature Γ<sub>2,t</sub> is seen from 13.6 to 15.5 h respectively.
- *Third Propagation*: A step-like variation is observed in voltage  $V_{4,t}$  from 6.0 to 9.2 h respectively.

The first propagation illustrates a step-like variation of voltage  $V_{2,t}$  collected from the floor of cells c1 and c2. The second propagation represents a rise in temperature  $\Gamma_{4,t}$ . This is the

impact of resilience shown by the impedance of cells c7 and c8 towards the faulty cell c2. The third propagation imitates a similar fluctuation pattern in voltage  $V_{4,t}$  like the propagated  $V_{2,t}$ . This is the reaction of temperature  $\Gamma_{2,t}$  and the floor of cells c5 and c6. All the propagations can be seen in Fig.7 (a)-(c).

*First Propagation:* The variation propagation of the reverse polarity in cell  $c^2$  was estimated. The first propagation consisted of a large variations across 8.0–14.2 h monitoring window. As a result, the estimation accuracy is impacted. While the window of 8.0–14.2 h could represent the impact of fault propagation, an effect due to the dynamic variations can be seen in a window of 1.0–1.5 h. However, the proposed method was able to estimate the variations with adequate precision. The PF [36] was slow in estimating the sharp variations as shown in Fig. 7 (d). The reverse polarity fault was detected and isolated appropriately as shown in Fig.7 (e)-(f). The threshold selected for residual was  $\pm 1$ .

Second Propagation: In the second propagation, the temperature sensor generated a large number of wiggles affecting window 16.2–19.8 h. Due to the high magnitude of variations, a semi-logarithmic plot was selected to monitor the estimation accuracy. The proposed scheme still computed accurate estimations. On the other hand, PF failed to capture the wiggles. This might be due to the congregation of sample measurements while predicting instant variations. The estimation comparison can be seen in Fig. 7 (g). Fault detection and isolation was proposed by using an interval-based adaptive threshold. As observed, the high variations in temperature are observed only in the positive values of temperature. Therefore, the threshold was active only in the positive scale. The evaluation can be seen in Fig.7 (h)-(i).

*Third Propagation:* Next, the third propagation was examined. Since, the propagation contained amplitudes and characteristics similar to first propagation, a semi-logarithmic plot was considered to monitor the variations as shown in Fig. 7 (j). The main stream PF lost the track assuming the independence of the observations without gaining any new information. The threshold selection algorithm was adequate to detect the variations by selecting a threshold of  $\pm 2$  while avoiding any false alarms. Subsequently, accurate detection signal was generated for fault isolation. The evaluation can be followed in Fig.7 (k)-(l).

#### **IV. CONCLUSIONS**

In this paper, an in-cell variation and propagation of a vehicle battery involved in V2G technologies has been analyzed. This is achieved by median expectation-based prediction approach to estimate the in-cell variations and split of current in the floor of arrays of cells. To enhance the analysis of these variations at the local level, the prediction structure is supported by the residual vector and hypothesis model. The proposed scheme has been demonstrated to improve the service life of the battery pack in EV, and thereby boost the effectiveness of power grid ancillary services. Estimation comparison of the scheme was made with two existing mainstream techniques of automotive lithium-ion batteries, extended Kalman filter and particle filter. In the future, studies will be conducted to quantitatively analyze the vehicular technology operations while considering the developed in-cell variations as an exogenous variable.

# Appendix

**Proof of Convergence for (20) and (21):** Since the currentsplit estimates of cell c1 and c2 are defined in (16), the estimation shall be converging if:

$$P_{I,\mathcal{CR},t|t}^{c1} \geq \mathbf{E}_{\mu_{1/2}} [(I_{\mathcal{CR},t|t}^{c1} - \hat{I}_{\mathcal{CR},t|t}^{c1})(I_{\mathcal{CR},t|t}^{c1} - \hat{I}_{\mathcal{CR},t|t}^{c1})'] (29)$$

$$P_{I,\mathcal{UC},t|t}^{c1} \geq \mathbf{E}_{\mu_{1/2}} [(I_{\mathcal{UC},t|t}^{c1} - \hat{I}_{\mathcal{UC},t|t}^{c1})(I_{\mathcal{UC},t|t}^{c1} - \hat{I}_{\mathcal{UC},t|t}^{c1})'] (30)$$

$$P_{I,\mathcal{CR},t|t}^{c2} \geq \mathbf{E}_{\mu_{1/2}} [(I_{\mathcal{CR},t|t}^{c2} - \hat{I}_{\mathcal{CR},t|t}^{c2})(I_{\mathcal{CR},t|t}^{c2} - \hat{I}_{\mathcal{CR},t|t}^{c2})'] (31)$$

$$P_{I,\mathcal{UC},t|t}^{c2} \geq \mathbf{E}_{\mu_{1/2}} [(I_{\mathcal{UC},t|t}^{c2} - \hat{I}_{\mathcal{CR},t|t}^{c2})(I_{\mathcal{CR},t|t}^{c2} - \hat{I}_{\mathcal{UC},t|t}^{c2})'] (32)$$
Considering (18), the difference between the fused uncorrelated covariance for cells c1, c2 and  $\mathbf{E} [(I_{\mathcal{UC},t|t}^{c} - \hat{I}_{\mathcal{UC},t|t}^{c2})(I_{\mathcal{UC},t|t}^{c2} - \hat{I}_{\mathcal{UC},t|t}^{c2})'] (I_{\mathcal{UC},t|t}^{c1} - \hat{I}_{\mathcal{UC},t|t}^{c2})'] (I_{\mathcal{UC},t|t}^{c1} - \hat{I}_{\mathcal{UC},t|t}^{c2})'] P_{I,t|t}^{c1}$ 

$$= P_{I,t|t}^{c} (P_{I,t|t}^{c1-1} P_{I,\mathcal{UC},t|t}^{c1} P_{I,t|t}^{c1-1} + P_{I,t|t}^{c2-1} P_{I,\mathcal{UC},t|t}^{c2} P_{I,t|t}^{c2-1}) P_{I,t|t}^{c1-1}$$

$$- P_{I,t|t}^{c2-1} \mathbf{E}_{\mu_{1/2}}^{c1} [(I_{\mathcal{UC},t|t}^{c2} - \hat{I}_{\mathcal{UC},t|t}^{c2})(I_{\mathcal{UC},t|t}^{c2} - \hat{I}_{\mathcal{UC},t|t}^{c2})] P_{I,t|t}^{c1-1}$$

$$+ P_{I,t|t}^{c2-1} \mathbf{E}_{\mu_{1/2}}^{c1-1} \mathbf{E}_{\mu_{1/2}}^{c1-1} [(I_{\mathcal{UC},t|t}^{c2-1} - \hat{I}_{\mathcal{UC},t|t}^{c2})(I_{\mathcal{UC},t|t}^{c2-1}) P_{I,t|t}^{c1-1}$$

$$+ P_{I,t|t}^{c2-1} \mathbf{E}_{\mu_{1/2}}^{c1-1} (P_{I,t|t}^{c2-1} - \hat{I}_{\mathcal{UC},t|t}^{c2}) (I_{\mathcal{UC},t|t}^{c2-1}) P_{I,t|t}^{c1-1}$$

$$= P_{I,t|t}^{c1} (P_{I,t|t}^{c1-1} + P_{I,t|t}^{c2-1} (P_{I,\mathcal{UC},t|t}^{c2-1} - \hat{I}_{\mathcal{UC},t|t}^{c2})) (I_{\mathcal{UC},t|t}^{c2-1}) P_{I,t|t}^{c1}$$

$$- \hat{I}_{\mathcal{U},t|t}^{c1}) P_{I,t|t}^{c1-1} + P_{I,t|t}^{c2-1} (P_{I,\mathcal{U},t|t}^{c2-1} - \hat{I}_{\mathcal{U},t|t}^{c2}) (I_{\mathcal{U},t|t}^{c2-1}) P_{I,t|t}^{c2-1}) P_{I,t|t}^{c2-1}) P_{I,t|t}^{c2-1} + P_{I,t|t}^{c2-1}) P_{I,t|t}^{c2-1}) P_{I,t|t}^{c2-1} + P_{I,t|t}^{c2-1} (P_{I,t|t}^{c2-1} - \hat{I}_{\mathcal{U},t|t}^{c2-1}) (P_{I,t|t}^{c2-1} - \hat{I}_{\mathcal{U},t|t}^{c2-1}))$$

 $(I_{\mathcal{UC},t|t}^{\mathcal{C}} - I_{\mathcal{UC},t|t}^{\mathcal{C}}) | P^{\mathcal{C}_{2}}) P_{I,t|t}^{\mathcal{C}} \ge 0$ (33) Similarly, considering (16) for correlated covariance, the convergence for the  $P_{I,\mathcal{C},t|t}^{\mathcal{C}} - \mathbf{E}_{\mu_{1/2}}[(I_{\mathcal{C},t|t}^{\mathcal{C}} - \hat{I}_{\mathcal{C},t|t}^{\mathcal{C}})(I_{\mathcal{C},t|t}^{\mathcal{C}} - \hat{I}_{\mathcal{C},t|t}^{\mathcal{C}})']$  can be achieved.

#### ACKNOWLEDGMENTS

The authors thank Associate Research Professor Qadeer Ahmed from Center for Automotive Research, The Ohio State University for his insights and suggestions.

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Fig. 7. Propagation of injected reverse polarity fault on cell  $c^2$  with its impact on a) voltage  $V_{2,t}$ , b) temperature  $\Gamma_{2,t}$ , and c) voltage  $V_{4,t}$ . Comparison of estimate for fault propagation and its evaluation of residual signal and fault isolation in d-f) voltage  $V_{2,t}$ , g-i) temperature  $\Gamma_{2,t}$ , j-l) voltage  $V_{4,t}$ , respectively

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